IBDP Mathematics Analysis and approaches (SL) Differentiation – Kinematic



Kinematic

Displacement s(t)Velocity v(t) = s'(t)Acceleration a(t) = v'(t)

Key words

At rest or change direction: v(t) = 0Constant velocity: a(t) = 0

v(t)	Meaning
= 0	At rest
> 0	Moving to the right
< 0	Moving to the left



1. A particle moves in a straight line with position given by $s(t) = t^3 - 3t + 1$, where t is the time in seconds, $t \ge 0$. Find the velocity of the particle at t = 1.

2. The velocity v ms^{-1} of a particle after t seconds is given by v(t) = $(0.1t + 0.5)^2 - 4$. Find the value of t when the acceleration is 0.9. IBDP Mathematics Analysis and approaches (SL) Differentiation – Kinematic



Paper 1

1. In this question, you are given that $\cos \frac{\pi}{3} = \frac{1}{2}$ and $\sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$. The displacement of an object from a fixed point, O is given by $s(t) = t - \sin 2t$ for $0 \le t \le \pi$.

(a) Find s'(t). In this interval, there are only two values of t for which the object is not moving. One value is $t = \frac{\pi}{6}$.

(b) Find the other value.

(c) Show that s'(t) > 0 between these two values of t.

(d) Find the distance travelled between these two values of t.

Paper 2



1. The population of deer in an enclosed game reserve is modelled by the function $P(t) = 210 \sin(0.5t - 2.6) + 990$, where t is in months, and t = 1 corresponds to 1 January 2014.

(a) Find the number of deer in the reserve on 1 May 2014.

(b) (i) Find the rate of the deer population on 1 May 2014.

(ii) Interpret the answer to part (i) with reference to the deer population size on 1 May 2014.

