

Function notation

1.
$$f(x) = 2x + 1$$

(a) Find f(3)(b) Find f(-2)

2.
$$f(x) = 3x^2 + 10$$

(a) Find f(2)(b) Find f(-1)



Inverse functions $f^{-1}(x)$

Reflect the function in the line y = xInterchange x and y

Two step

- 1. Swop x, y
- 2. Make y subject

1. f(x) = 3x + 2

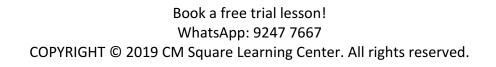
(a) Find the inverse function $f^{-1}(x)$.

(b) Sketch the graph of f(x) and $f^{-1}(x)$ on the same axes.



2. f(x) = 4x - 3

- (a) Find the inverse function.
- (b) Sketch the graph of f(x) and $f^{-1}(x)$ on the same axes.



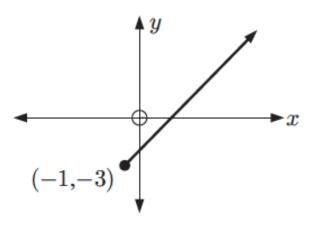
Domain

Set of x values in the relation

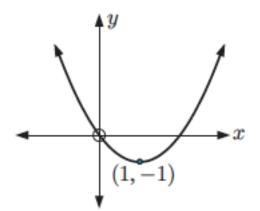
Range

Set of y values in the relation

Example



Domain $\{x | x \ge 1\}$ Range is $\{y | y \ge -3\}$

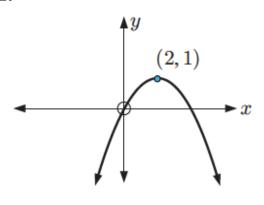


Domain $\{x | x \in \mathbb{R}\}$ Range is $\{y | y \ge -1\}$

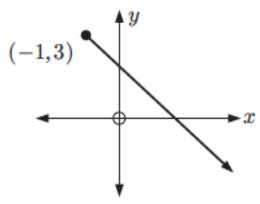




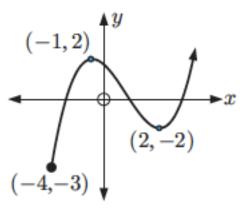
For each of the following graphs state the domain and range. 1.













Axis of symmetry

The equation of the axis of symmetry is x = C.

Axis of symmetry is the vertical line splitting the graph into half.

Quadratic form: $y = ax^2 + bx + c$

Axis of symmetry is $x = \frac{-b}{2a}$



1. The x-intercepts of a quadratic function are 1 and 9. Find the equation of axis of symmetry.

2. The x-intercepts of a quadratic function are -2 and 6. Find the equation of axis of symmetry.

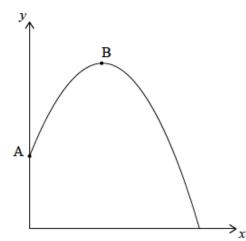


Exercise

1. Bella throws a ball from the top of a wall onto flat horizontal ground.

The path of the ball is modelled by the quadratic curve $y = 2 + 4x - x^2$, where x represents the horizontal distance the ball is thrown and y represents the height of the ball above the ground. All distances are measured in metres.

The wall lies along the y-axis. The curve intersects the y-axis at point A and has its vertex at point B.



(a) Write down the height in metres from which the ball was thrown.

(b) Calculate the maximum height, above the ground, reached by the ball.

(c) Find the horizontal distance from the base of the wall to the point at which the ball hits the ground.





2. Consider the quadratic function $f(x) = ax^2 + bx + 22$. The equation of the line of symmetry of the graph y = f(x) is x = 1.75. (a) Using only this information, write down an equation in terms of a and b.

The graph intersects the x-axis at the point (-2, 0). (b) Using this information, write down a second equation in terms of a and b.

(c) Hence find the value of *a* and of *b*.

The graph intersects the *x*-axis at a second point, P. (d) Find the *x*-coordinate of P.